		STUDY MODULE D	ES	CRIPTION FORM			
	f the module/subject hastic methods	and mathematical statisti	cs	Code 1010342621010347255			
Field of	study			Profile of study (general academic, practical	)	Year /Semester	
Math	nematics			general academic	<i>'</i>	1/2	
Elective	path/specialty			Subject offered in:		Course (compulsory, elective)	
Cuela a		odelling in applied sciend		Polish		obligatory	
Cycle of			FOI	m of study (full-time,part-time)			
	Second-c	ycle studies		full-	tim	e	
No. of h						No. of credits	
Lectur	Classes			Project/seminars:	-	4	
Status o	of the course in the study	program (Basic, major, other) other	(	university-wide, from another		ty-wide	
Educati	on areas and fields of sci				CI 31	ECTS distribution (number	
						and %)	
technical sciences						4 100%	
	Technical scie	ences				4 100%	
Resp	onsible for subje	ect / lecturer:					
Kamil Świątek, Ph.D. email: kamil.swiatek@put.poznan.pl tel. 61665-2816 Wydział Elektryczny							
ul. F	Piotrowo 3A, 60-965 P	oznań					
Prere	equisites in term	s of knowledge, skills an	d se	ocial competencies:	:		
1	Knowledge	knows the basic concepts of sub	oject	of Probability and statistic	S		
2	Skills	has a ability to think logically (student formulates new facts from a previously known facts)					
3	Social competencies	knows the limits of his own knowledge and understands the need for further education					
Assu	mptions and obj	ectives of the course:					
stocha the stu stocha	stic processes and to dent will get to know t stic differentials (stoch stic differential equation		alcul ill ac exan	ate some characteristics of quire the ability to determine whether some process	of tho ne th s is a	ese processes. Furthermore estochastic integrals and a solution to a given	
	-	mes and reference to the	ed	ucational results for	raf	ield of study	
	vledge:						
mather	matical models, which	ion of mathematical theories, can describe phenomena from other of	disci	plines - [K_W03]	o con	struct and analyze simple	
2. knov Skills		of the known branches of mather	natio	cs - [K_W04]			
		y space; is able to build and analy	/70 9	mathematical model of so	cienti	fic experiment of random	
phenor	mena - [K_U30]	mples of discrete and continuous					
experir		cal models in which those distribut					
theore	<ol> <li>is able to determine the parameters of distribution function of discrete and continuous random variables; can apply the limi theorems and laws of large numbers to estimate probability of some random variables - [K_U33]</li> </ol>						
sample	e - [K_U34]	al characteristics of population and	the	ir counterparts which can b	be ca	alculate by using a probability	
Socia	al competencies:						

# Social competencies:

1. is able to accurately formulate questions in order to deepen their understanding of given topic or in order to find the missing pieces of reasoning - [K\_K02]

2. understands and appreciates the importance of intellectual honesty in the activities of their own and other people; proceeds ethically - [K\_K04]

#### Assessment methods of study outcomes

#### Lectures:

- Assessment of the knowledge and skills based on the written exam.

Laboratories:

- Assessment of the knowledge and skills based on tests, which are carried out in the middle of the semester and during the last classes.

## Course description

Basic concepts of the theory of stochastic processes: stochastic process, sample path of stochastic process, interpretation of a stochastic process as a random variable, interpretation of a stochastic process as a function of two variables, measurability of stochastic process, filtration, class of adapted processes, class of indistinguishable processes, modification of the stochastic process, Kolmogorov's continuity theorem, continuity types of the stochastic process (continuity with probability one, continuity in probability, mean-square continuity).

Probabilistic description of the stochastic process: examples of processes which are analytical defined, some characteristics of sums and products of stochastic processes, canonical form of the stochastic processes, processes with independent increments, telegraphic signals (synchronous processes, asynchronous processes).

Markov process: definition of Markov process, examples of Markov processes, Markov chain, certain examples of the problems of mass service.

Poisson process: definition of Poisson process, properties of Poisson process.

Some characteristics of differentiable processes and integrable processes (convergence in mean-square sense, mean-square derivative, mean-square integral, ergodicity), and elements of spectral analysis of stationary stochastic processes (spectral density).

Martingales: definitions of discrete-time martingale and continuous-time martingale, examples of martingales, verification whether the process is a martingale, transformation of the known stochastic processes to martingales, Doob's martingale inequality, definition of submartingale and supermartingale, example of submartingale and supermartingale in game theory.

Markov time: definition and properties of Markov time, examples of Markov time, definition and example of the first passage time of stochastic process to the set, definition and properties of stopping time, definition and properties of local martingale.

Brownian motion: definition of Brownian motion, definition of standard Brownian motion, properties of standard Brownian motion, properties of sample path of Brownian motion, brownian motion as a square integrable martingale.

Wiener process: definition of Wiener process, Levy's theorem, examples of Wiener processes, Wiener process as a martingale, examples of stochastic processes determined by transformation of Wiener process, which turn out to be a martingales, example of application of the Wiener process into theory of financial mathematics - geometric Brownian motion (exponential Brownian motion).

Construction of Itô integral: white noise, definition of simple function, comparison of the construction of Itô integral with the construction of Riemanna-Stieltjesa integral, non-anticipating processes, predictable processes, Itô isometry, definition of Itô integral, example of calculation of stochastic integral based on the definition of Itô integral, properties of stochastic Itô integral.

Itô formula: definition of Itô process, definition of stochastic differential, definition of diffusion process, Itô's lemma, application of the Itô formula (calculation of stochastic integrals and stochastic differentials, and verification whether some stochastic process is a solution to a given stochastic differential equation).

Applied methods of education:

- lectures - theory presented in connection with the current knowledge of students,

- laboratories - computational experiments.

#### Update date: 06.02.2017

## **Basic bibliography:**

1. R. Sz. Lipcer, A. N. Sziriajew, Statystyka procesów stochastycznych: filtracja nieliniowa i zagadnienia pokrewne, PWN, Warszawa 1981.

2. A. Pieniążek, J. Weiss, A. Winiarz, Procesy stochastyczne w problemach i zadaniach, Wydaw. Politechniki Krakowskiej im. Tadeusza Kościuszki, Kraków 2000.

3. A. Plucińska, E. Pluciński, Probabilistyka: rachunek prawdopodobieństwa, statystyka matematyczna, procesy stochastyczne, WNT, Warszawa 2000.

## Additional bibliography:

1. B. Oksendal, Stochastic differential equations. An introduction with applications, Springer-Verlag, Berlin Heidelberg New York 2000.

2. Z. Brzezniak, T. Zastawniak, Basic stochastic processes. A course through exercises, Springer-Verlag, London 2002.

3. A. Iwanik, J. K. Misiewicz, Wykłady z procesów stochastycznych z zadaniami. Cz. 1: Procesy Markowa, Oficyna Wydaw. Uniwersytetu Zielonogórskiego, Zielona Góra 2009.

Result of average stud	dent's workload	
Activity		Time (working hours)
1. Participation in lectures		30
2. Participation in laboratories	30	
3. Preparation for each laboratories	20	
4. Preparation for written test	12	
5. Assessment classes	4	
6. The written exam		4
7. Consultations		4
Student's wo	orkload	
Source of workload	hours	ECTS
Total workload	104	4
Contact hours	72	3
Practical activities	30	1